

Comparison of pressure vessel codes

Why do the codes differ and How do they differ

Presented by: Ray Delaforce

COMPARISON of the various pressure vessel codes

These are the codes we are going to compare:

- ASME Section VIII, Division 1
- ASME Section VIII, Division 2
- PD 5500
- EN 13445 Part 3

But first we look at the most fundamental requirement

What is the ALLOWABLE STRESS ?

This is the primary stress we must not exceed

A PRIMARY stress results from internal pressure

There are SECONDARY stresses – we do not discuss them

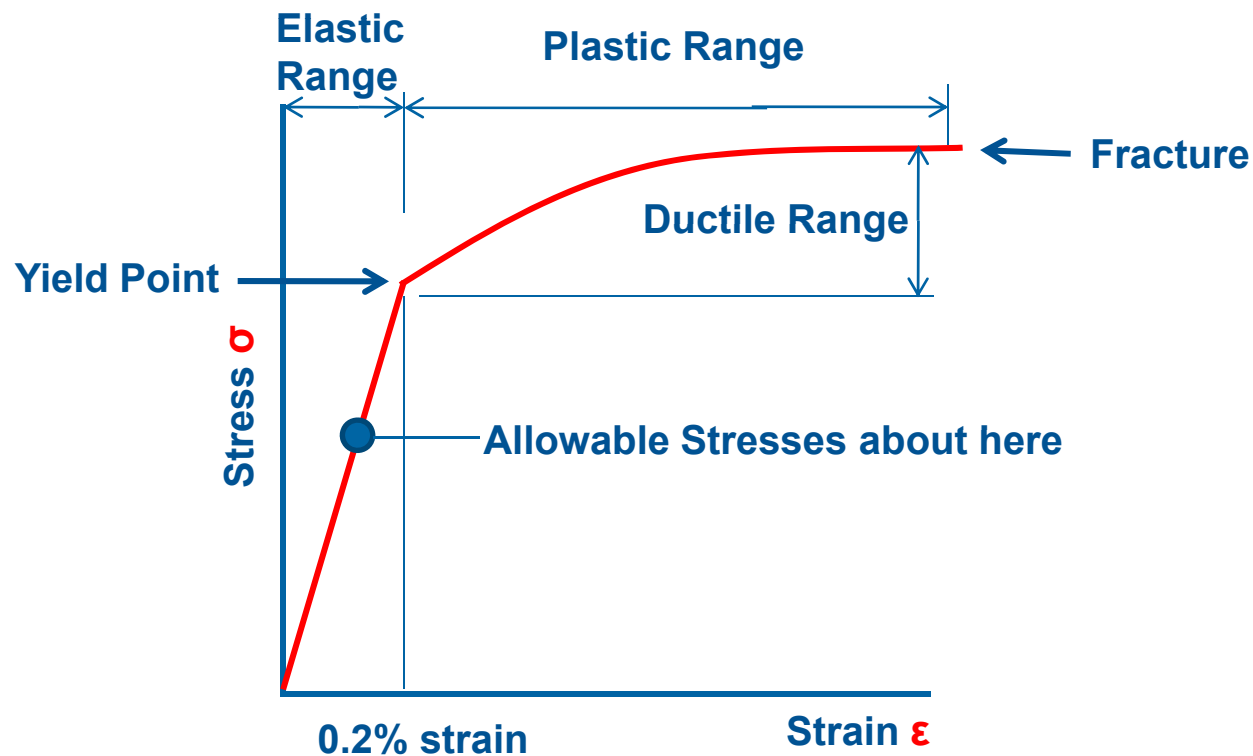
COMPARISON of the various pressure vessel codes

We first look at a couple of important material properties

Let us look at the Stress-Strain diagram – we get a lot of information

Collapse can occur when we reach the yield point

Let us look at the important features of our steel



COMPARISON of the various pressure vessel codes

Consider steel: UTS = 70 000 psi (482 MPa) Yield 38000 psi (262 MPa)

Let us look at the Stress-Strain diagram – we get a lot of information

Collapse can occur when we reach the yield point

Let us look at the important features of our steel

There are three important features we must consider

- | | |
|--|-------------------------|
| 1. There is the limit of proportionality | Yield Point 0.2% strain |
| 2. The Ultimate Tensile Strength (UTS) | When fracture occurs |
| 3. The Ductility = Yield / UTS | Must be less than 1.0 |

There is a 4th one – Creep which occurs at higher temperatures

COMPARISON of the various pressure vessel codes

Allowable stress is base on these characteristics of the metal

ASME Section VIII Division 1

S = smaller of: **UTS / 3.5** or **Yield / 1.5** = 20 000 psi (138 MPa)

ASME Section VIII Division 2

Sm = smaller of: **UTS / 2.4** or **Yield / 1.5** ← 25 300 psi (174 MPa)

EN 13445

Both based on PED European requirements

f = smaller of: **UTS / 2.4** or **Yield / 1.5** ← 25 300 psi (174 MPa)

PD 5500

f = smaller of: **UTS / 2.35** or **Yield / 1.5** = 25 300 psi (174 MPa)

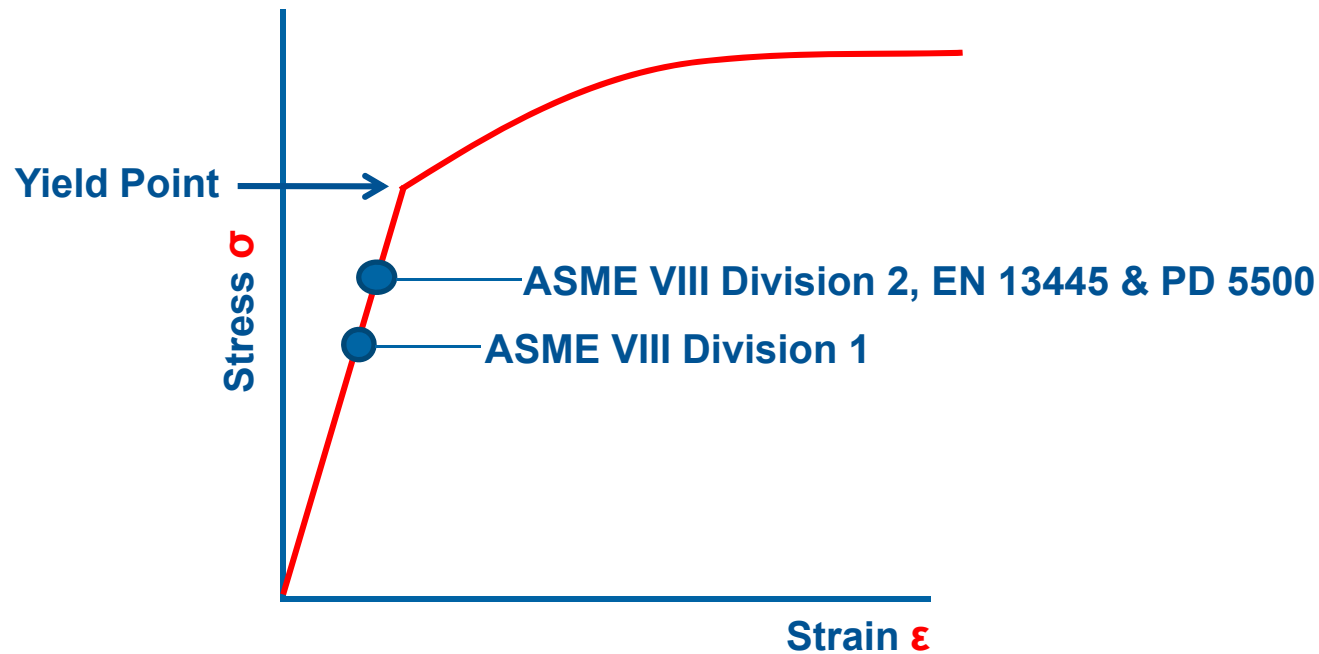
We consider Carbon Steel for simplicity

COMPARISON of the various pressure vessel codes

We look at this on the Stress Strain diagram

ASME VIII, Division 1 has a larger safety margin – safer

This code is still the favoured code throughout the World



COMPARISON of the various pressure vessel codes

Let us now look at a typical calculation – the cylindrical shell

Here are the basic dimensions We shall ignore joint efficiency **E (z)**

We now do the calculation for the cylinder:

P = 300 psi (207 MPa)

D = 60 ins (1 524 mm)

S(f) = 20 000 psi (174 MPa)

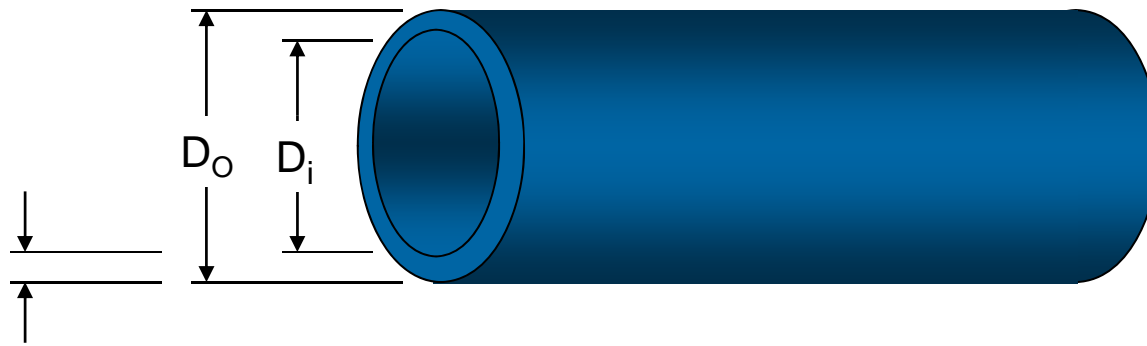
By ASME VIII Division 1

$$t = \frac{P \cdot D}{2 \cdot S - 1.2P} \quad t = 0.454 \text{ in (11.534 mm)}$$

By ASME VIII Division 2

$$t = \frac{D}{2} \cdot \left(\exp\left(\frac{P}{S}\right) - 1 \right) \quad t = 0.453 \text{ in (11.516 mm)}$$

By EN 13445



t ASME e EN 13445 & PD5500

COMPARISON of the various pressure vessel codes

Let us now look at a typical calculation – the ~~Elliptical Head~~ **Cylindrical Shell**

Here are the basic dimensions We shall ignore joint efficiency **E**

We now do the calculation for the cylinder:

P = 300 psi (207 MPa)

D = 60 ins (1 524 mm)

S(f) = 20 000 psi (174 MPa)

$$t = \frac{P \cdot D}{2 \cdot S}$$

That is why the differences are so small – the formulae are nearly the same !

This formula looks odd, but is actually just about the same as the others

By ASME VIII Division 1

$$t = \frac{P \cdot D}{2 \cdot S - 1.2P} \quad t = 0.454 \text{ in (11.534 mm)}$$

By ASME VIII Division 2

$$t = \frac{D}{2} \cdot \left(\exp\left(\frac{P}{S}\right) - 1 \right) \quad t = 0.453 \text{ in (11.516 mm)}$$

By EN 13445

$$e = \frac{P \cdot D}{2 \cdot f - P} \quad t = 0.453 \text{ in (11.516 mm)}$$

By PD 5500

$$e = \frac{P \cdot D}{2 \cdot f - P} \quad t = 0.453 \text{ in (11.516 mm)}$$

COMPARISON of the various pressure vessel codes

Let us now look at a typical calculation – the ~~Elliptical Head~~ **Cylindrical Shell**

Here are the basic dimensions We shall ignore joint efficiency **E**

We now do the calculation for the cylinder:

By ASME VIII Division 1

Cylinder based on the equilibrium equation

$$t = \frac{P \cdot D}{2 \cdot S - 1.2P}$$

$$t = 0.454 \text{ in (11.534 mm)}$$

By ASME VIII Division 2

$$t = \frac{P \cdot D}{2 \cdot S}$$

That is why the differences are so small – the formulae are nearly the same !

$$t = \frac{D}{2} \cdot \left(\exp\left(\frac{P}{S}\right) - 1 \right)$$

$$t = 0.453 \text{ in (11.516 mm)}$$

By EN 13445

$$e = \frac{P \cdot D}{2 \cdot f - P}$$

$$t = 0.453 \text{ in (11.516 mm)}$$

By PD 5500

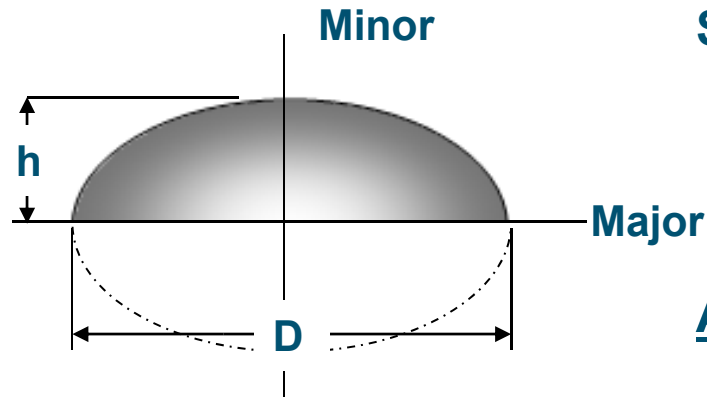
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This formula looks odd, but is actually just about the same as the others

COMPARISON of the various pressure vessel codes

Let us now look at a typical calculation – the Elliptical Head



Shape is based on true ellipse

$$D/2h = 2$$

ASME Division 2 – simplified calculation

$$P = 300 \text{ psi (207 MPa)}$$

$$D = 60 \text{ ins (1 524 mm)}$$

$$S(f) = 20\,000 \text{ psi (138 MPa)}$$

$$t = \frac{P \cdot D}{2 \cdot S - 0.2 \cdot P}$$

$$t = 0.451 \text{ in}$$

$$t = 11.447 \text{ mm}$$

Head formula almost identical to the cylinder formula:

Cylinder:

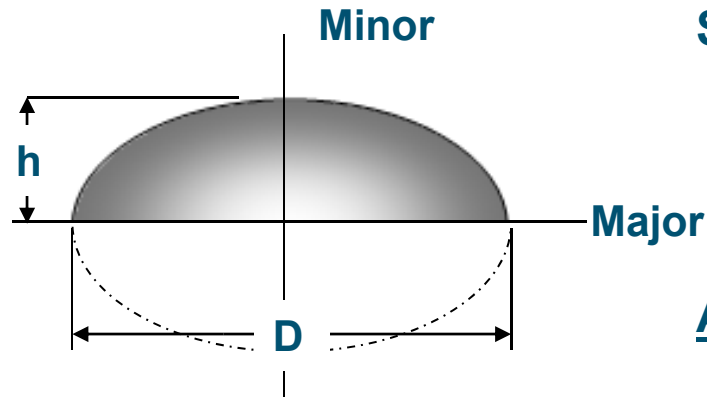
$$t = \frac{P \cdot D}{2 \cdot S - 1.2P}$$

Elliptical head:

$$t = \frac{P \cdot D}{2 \cdot S - 0.2 \cdot P}$$

COMPARISON of the various pressure vessel codes

Let us now look at a typical calculation – the Elliptical Head



Shape is based on true ellipse

$$D/2h = 2$$

ASME Division 2 – complicated calc.

P = 300 psi (207 MPa)

D = 60 ins (1 524 mm)

S(f) = 25 300 psi (174 MPa)

Division 2 allows higher stress

1 There are many steps to do

2 Cannot calculate **t** directly
only **P**

On the next slide we show the calculation per *PV Elite*

COMPARISON of the various pressure vessel codes

This is the calculation using *PV Elite* - ASME Division 2

The Elliptical head is transformed in equivalent Torispherical Head

Elliptical Head From 10 To 20 SA-516 70 , Fig. 3.7M Curve B at 20 C

2:1 Elliptical head

Head Calculation - Section 4.3.6 (and Section 4.3.7 for Ellipsoidal Head)

Computed Minimum Required Thickness [t]:

$$\begin{aligned} t_r &= 2.7226 \text{ mm} \\ t &= t_r + c_i + c_o \\ &= 2.7226 + 3.1750 + 0.0000 \\ &= 5.8976 \text{ mm} - \text{see below for the derivation} \end{aligned}$$

For and Elliptical heads: Compute [h, k, r,] per 4.3.7.1

$$h = D / (2 * \text{Aspect Ratio}) + c = 1524.000 / (2 * 2.000) + 3.175 = 384.1750 \text{ mm}$$

$$k = D_{\text{corr}} / (2 * h) = 1530.350 / (2 * 384.175) = 1.9917$$

$$r = D_{\text{corr}} * (0.5 / k - 0.08) = 1530.350 * (0.5 / 1.992 - 0.08) = 261.7470 \text{ mm}$$

$$L = D_{\text{corr}} * (0.44 * k + 0.02) = 1530.350 * (0.44 * 1.992 + 0.02) = 1371.75$$

Crown radius

Knuckle radius

COMPARISON of the various pressure vessel codes

This is the calculation using *PV Elite* - ASME Division 2

Next we must calculate some geometry factors

$$\begin{aligned}\text{BetaTh} &= \text{acos}[(0.5 \cdot D - r) / (L - r)] = \text{acos}[(0.5 \cdot 1530.3 - 261.75) / (1371.75)] \\ &= 1.1001 \text{ radians} - \text{Equation 4.3.8}\end{aligned}$$

$$\begin{aligned}\text{PhiTh} &= \text{sqrt}(L \cdot t) / r \\ &= \text{sqrt}(1371.750 \cdot 2.723) / 261.747 \\ &= 0.2335 \text{ radians} - \text{Equation 4.3.9}\end{aligned}$$

PhiTh < BetaTh, Thus:

$$\begin{aligned}\text{Rth} &= (0.5 \cdot D - r) / \cos(\text{BetaTh} - \text{PhiTh}) + r \\ &= (0.5 \cdot 1530.350 - 261.747) / \cos(1.100 - 0.233) + 261.747 \\ &= 1039.3262 \text{ mm} - \text{Equation 4.3.10}\end{aligned}$$

Step 4: Compute Coefficients: Equations 4.3.12 to 4.3.15 [C1 and C2]:

$r/D > 0.08$, Thus:

$$\begin{aligned}\text{C1} &= 0.692 \cdot (r / D) + 0.605 \\ &= 0.692 \cdot (261.747 / 1530.350) + 0.605 \\ &= 0.7234 - \text{Equation 4.3.13}\end{aligned}$$

$$\begin{aligned}\text{C2} &= 1.46 - 2.6 \cdot (r/D) = 1.46 - 2.6 \cdot (261.747 / 1530.350) \\ &= 1.0153 - \text{Equation 4.3.15}\end{aligned}$$

COMPARISON of the various pressure vessel codes

This is the calculation using *PV Elite* - ASME Division 2

Even more geometry and other factors.and.more – lots of factors

Step 5: Compute pressure to produce knuckle elastic buckling[Peth]:

$$\begin{aligned} &= C1 * Et * t^3 / (C2 * Rth * (0.5 * Rth - r)) \\ &= 0.723 * 202786.203 * 8.177^3 / \\ &\quad (1.018 * 912.771 * (0.5 * 912.771 - 259.080)) \\ &= 53.4404 \text{ MPa} - \text{Equation 4.3.16} \end{aligned}$$

Step 6: Compute Internal Pressure for max stress in knuckle equals yield [Py]:

$$C3 = Sy = 262.010 \text{ MPa (Not in the creep range - 4.3.6.1(f))}$$

$$\begin{aligned} Py &= C3 * t / (C2 * Rth * (0.5 * Rth / r - 1)) \\ &= 262.010 * 8.177 / (1.018 * 912.771 * (0.5 * 912.771 / 259.080 - 1)) \\ &= 3.0275 \text{ MPa} - \text{Equation 4.3.17} \end{aligned}$$

Step 7: Value of Internal Press. resulting in buckling of knuckle [G and Pck]:

$$G = Peth / Pv = 53.440 / 3.027 = 17.6518$$

COMPARISON of the various pressure vessel codes

This is the calculation using *PV Elite* - ASME Division 2

Even more geometry and other factors and more – lots of factors

$G > 1$, Thus:

$$\begin{aligned} P_{ck} &= ((0.77508G - 0.20354G^2 + 0.019274G^3) / \\ &\quad (1 + 0.19014G - 0.089534G^2 + 0.0093965G^3)) P_y \\ &= ((0.77508*17.652 - 0.20354*17.652^2 + 0.019274*17.652^3) / \\ &\quad (1 + 0.19014*17.652 - 0.089534*17.652^2 + 0.0093965*17.652^3)) * 3.027 \\ &= 6.0538 \text{ MPa} - \text{Equation 4.3.19} \end{aligned}$$

Step 8: Compute Allowable Pressure base on buckling of knuckle [Pak]:

$$= P_{ck} / 1.5 = 6.054 / 1.5 = 4.0359 \text{ MPa} - \text{Equation 4.3.21}$$

Step 9: Compute allowable pressure based on rupture of crown [Pac]:

$$\begin{aligned} &= 2 * S * E / (L / t + 0.5) \\ &= 2 * 174.000 * 1.000 / (1371.600 / 8.177 + 0.5) \\ &= 2.0684 \text{ MPa} - \text{Equation 4.3.22} \end{aligned}$$

Step 10: Compute final pressure [Pa]:

$$\begin{aligned} &= \text{Min}(P_{ak}, P_{ac}) = \text{Min}(4.036, 2.068) \\ &= 2.0684 \text{ MPa} - \text{Equation 4.3.23: (same as original design pressure)} \end{aligned}$$

Finally we end up with our starting pressure

PV Elite does an iterative calculation to end up with the pressure

COMPARISON of the various pressure vessel codes

This is the calculation using *PV Elite* - ASME Division 2

We had to start the calculate with a 'guess' thickness **t**

Computed Minimum Required Thickness [t]:

$$\begin{aligned} t_r &= 8.1767 \text{ mm} \\ t &= t_r + c_i + c_o \\ &= 8.1767 + 0.0000 + 0.0000 \\ &= 8.1767 \text{ mm} - \text{see below for the derivation} \end{aligned}$$

And we ended up with our starting pressure

Step 9: Compute allowable pressure based on rupture of crown [Pac]:

$$\begin{aligned} &= 2 * S * E / (L / t + 0.5) \\ &= 2 * 174.000 * 1.000 / (1371.600 / 8.177 + 0.5) \\ &= 2.0684 \text{ MPa} - \text{Equation 4.3.22} \end{aligned}$$

We have to use a computer to do this calculation !

The computed thickness is **t = 0.3219 in** **t = 8.1767 mm**

COMPARISON of the various pressure vessel codes

This is the calculation using *PV Elite* - ASME Division 2

EN 13445 has a similar method – slightly less complicated than ASME

Required Crown Thickness due to Internal Pressure, see Figure 7.5-3 [es]:

$$\begin{aligned}
 &= P * R / (2 * f * z - 0.5 * P) \\
 &= 2.068 * 1371.6 / (2 * 174.000 * 1.00 - 0.5 * 2.068) \\
 &= 8.1767 \text{ mm}
 \end{aligned}$$

$$\begin{aligned}
 e_y &= \text{Beta} * P * (0.75 * R + 0.2 * D_i) / f = 0.62 * 2.1 * (0.75 * 1371.6 + 0.2 * 1524.0) / \\
 &174.0000 = 9.8619 \text{ mm}
 \end{aligned}$$

$$\begin{aligned}
 e_b &= (0.75R + 0.2D_i) * ((P/111 * f_b) * (D_i/r)^{(0.825)})^{(1/1.5)} \\
 &= (0.75 * 1371.60 + 0.2 * 1524.00) * \\
 &(2.07/111 * 156.67) * (1524.00/259.08)^{(0.825)}^{(1/1.5)} \\
 &= 8.5466 \text{ mm}
 \end{aligned}$$

Computed Head Thickness per EN13445 - 7.5.4:

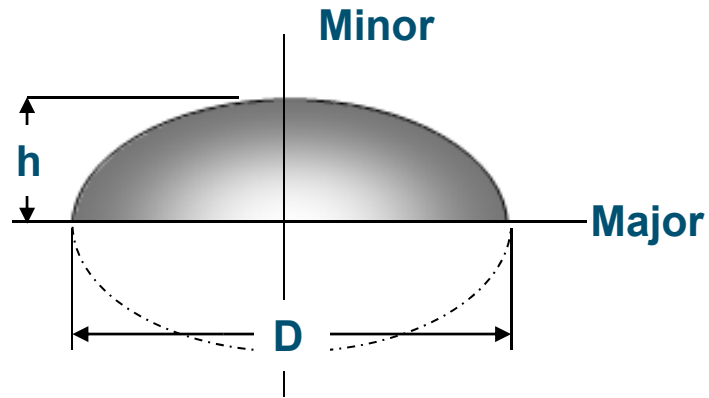
$$\begin{aligned}
 &= \text{Max}(e_s, e_b, e_y) + c + c_{ext} = \text{Max}(8.1767, 8.5466, 9.8619) + 0.0000 + 0.0000 \\
 &= 9.8619 + 0.0000 + 0.0000 = 9.8619 \text{ mm}
 \end{aligned}$$

... ..

The final computed thickness is: **t = 0.3886 in** **t = 9.8619 mm**

COMPARISON of the various pressure vessel codes

The method of computing the head by PD 5500 is very different



P = 300 psi (207 MPa)

D = 60 ins (1 524 mm)

f = 25 300 psi (174 MPa)

1 Calculate **h / D = 0.25**

2 Calculate **P / f = 0.119**

PD 5500 uses a graphical solutions – like this

COMPARISON of the various pressure vessel codes

Here is the Graph used to compute this head thickness

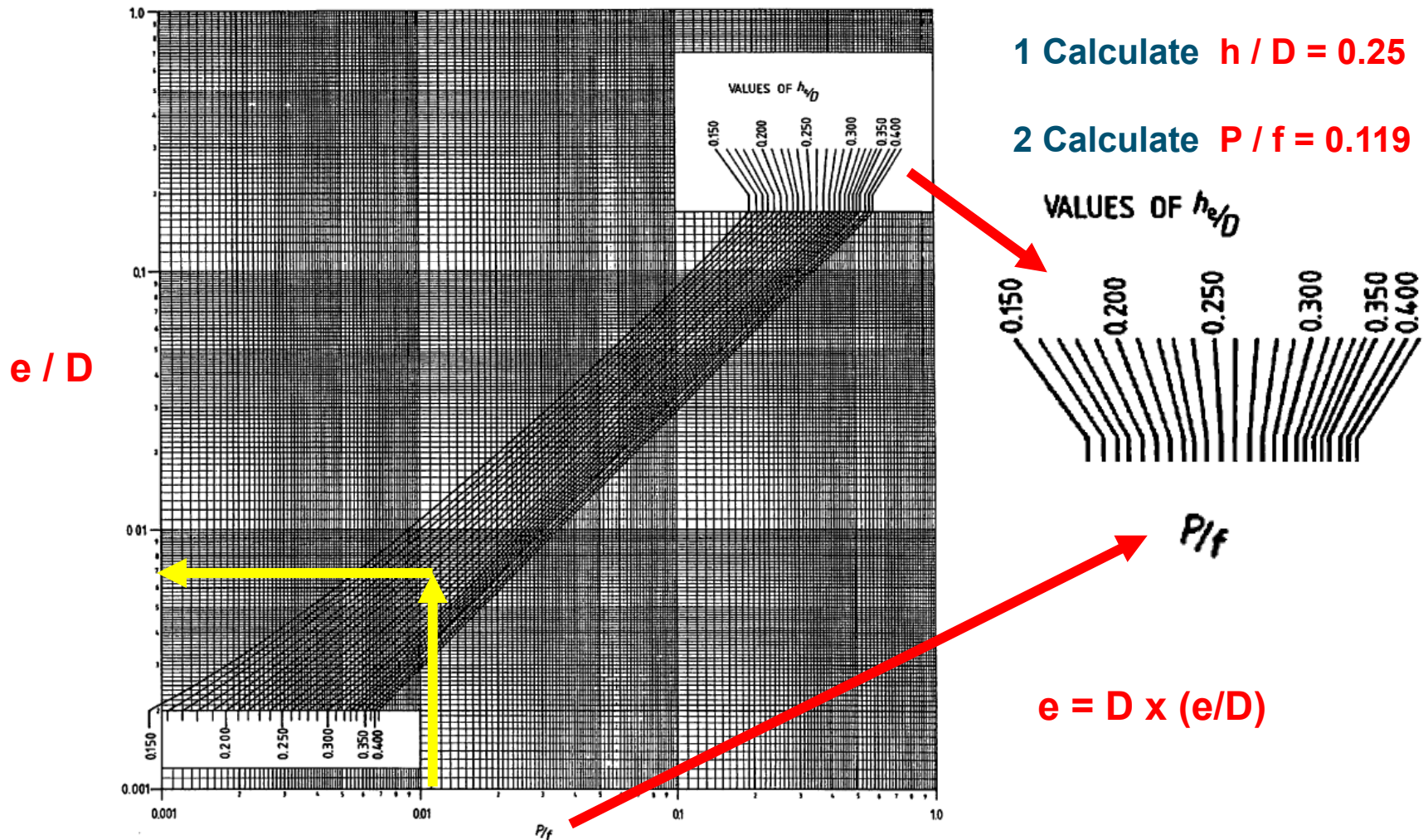


Figure 3.5-2 — Design curves for unpierced dished ends

COMPARISON of the various pressure vessel codes

This is the calculation using *PV Elite*

Internal Pressure Calculation Results :

British Standard PD 5500:2009

Elliptical Head From 10 To 20 BS1501-151,430A at 20 F

Thickness Due to Internal Pressure (TR):

```
= Values_Used_Min( HT, HE1, HE2 ), P/f, he/D, D Per 3.5.2 Domed Ends  
= Values_Used_Min(15.40,99999.00,99999.00),0.01186,0.2533,60.80  
= 0.3792 + 0.0000 = 0.3792 in
```

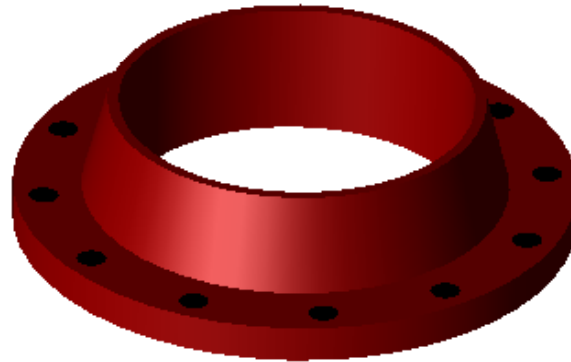
t = 0.3792 in t = 9.6317 mm

Each code has its own way of computing a head – and other parts

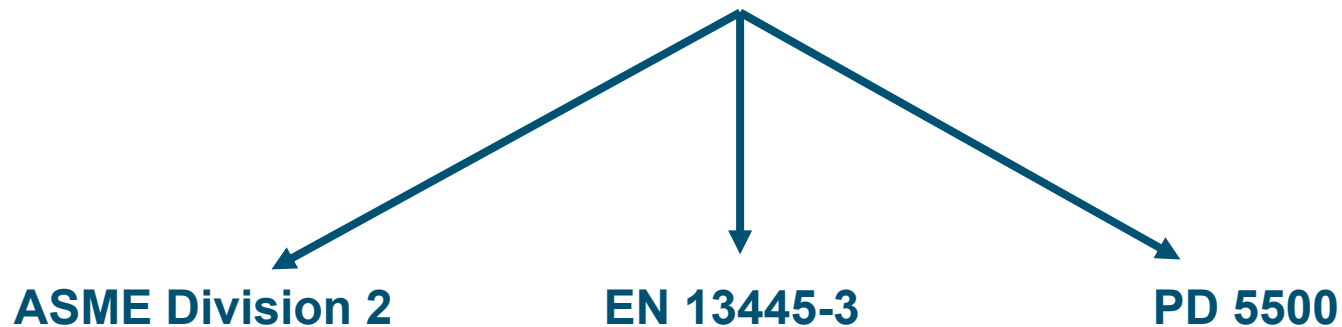
But, where do codes ‘borrow’ procedures from other codes ?

COMPARISON of the various pressure vessel codes

Codes 'Copy' codes – some examples Flange analysis

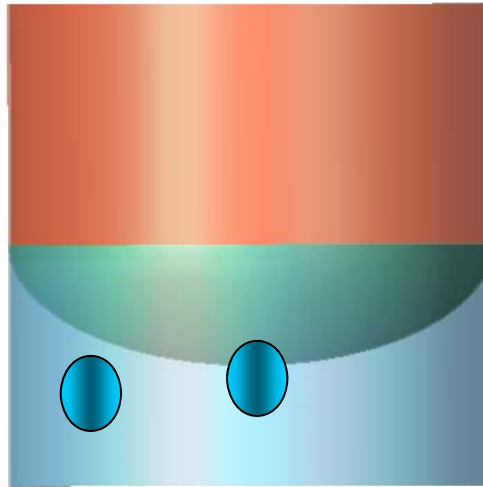


ASME Division 1



COMPARISON of the various pressure vessel codes

Codes 'Copy' codes – some examples Access openings in skirt



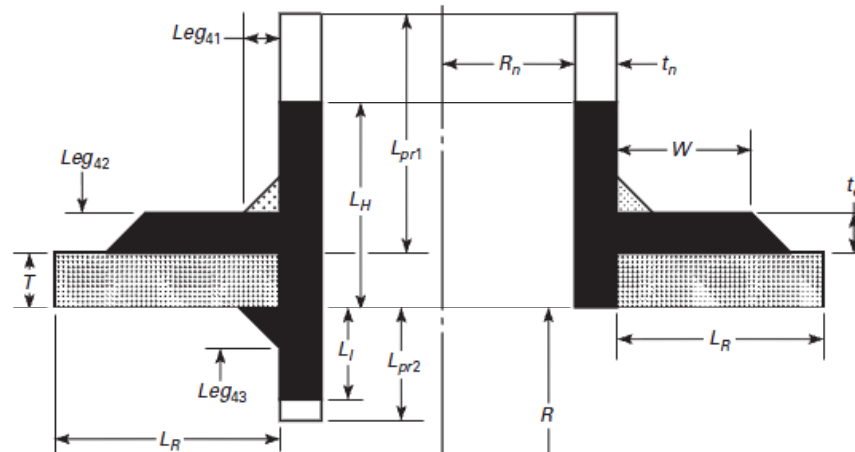
AD Merblatter (AD 2000)



EN 13445-3

COMPARISON of the various pressure vessel codes

Codes 'Copy' codes – some examples Pressure – Area method



PD 5500

ASME Division 1

ASME Division 2

EN 13445-3

Each of the codes has modified the method – same principle

COMPARISON of the various pressure vessel codes

We have looked at various codes of construction

We have learned some important issues

1. **ASME VIII Division 1 requires thicker metal – high safety factor**
2. **The other codes we discussed use thinner metal, but the allowable stresses are nearer the yield point – less safety**
3. **Some procedure in the codes have been ‘borrowed’ from other codes**
4. **ASME VIII Division 2 and EN 13445 are based on the PED (European Pressure Equipment Directive)**

It is hoped you got some value out of this webinar